

A Framework for Exploring Multidimensional Data with 3D Projections

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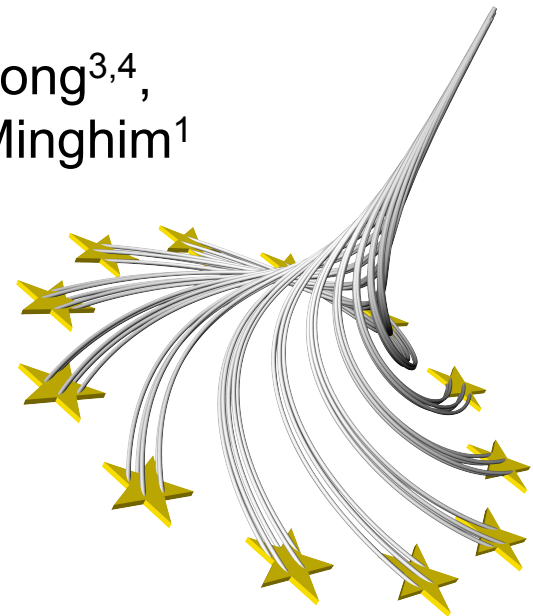
1University of São Paulo, São Carlos, Brazil

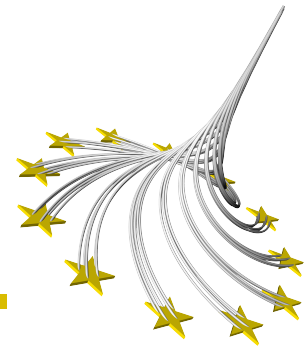
2 University of Utah, USA

3 Jacobs University, Bremen, Germany

4 University of Transport and Communication Hanoi, Vietnam

5 Chemnitz University of Technology, Germany

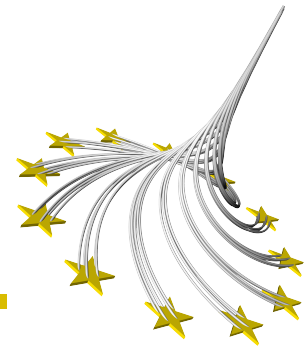




Introduction

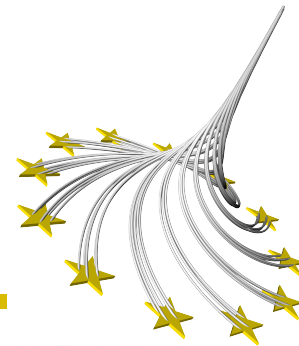
- MDS for visualization
- Intuitively 3D is better at group separation
- But difficult to interact with
- Framework to create and interact with 3D data projections

Outline

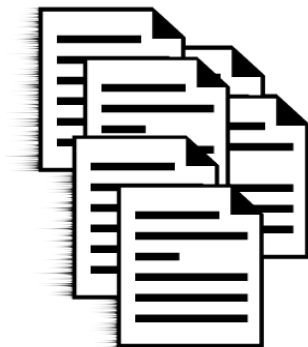


- Motivation
- Projections Algorithms
 - Quantitative Analysis
- 3D Cluster Visualization
- The Framework
- User Studies
 - 3D vs. 2D LSP
 - Surfaces Evaluation
- Conclusions

Motivation



Datasets



Document Collection

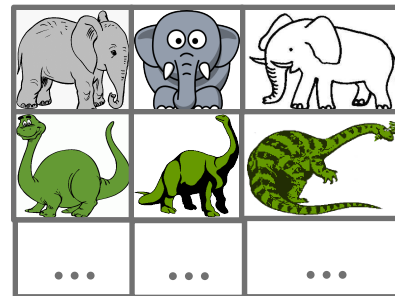


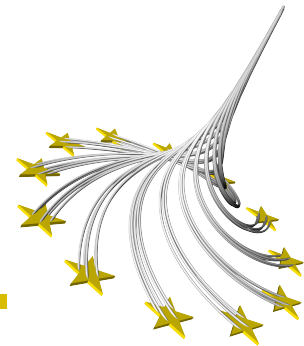
Image Collection

	XY	1	2	3	4	5	6	7	8	9	10	total
1	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
2	2	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
3	3	0.00	10.61	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	10.61
4	4	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
5	5	0.00	0.00	79.43	0.00	0.00	0.00	0.00	0.00	0.00	0.00	79.43
6	6	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
7	7	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
8	8	0.00	0.00	0.00	0.00	0.00	0.00	73.41	0.00	0.00	0.00	73.41
9	9	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
10	10	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
11	Sum	0.00	10.61	79.43	0.00	0.00	0.00	73.41	0.00	0.00	0.00	163.45

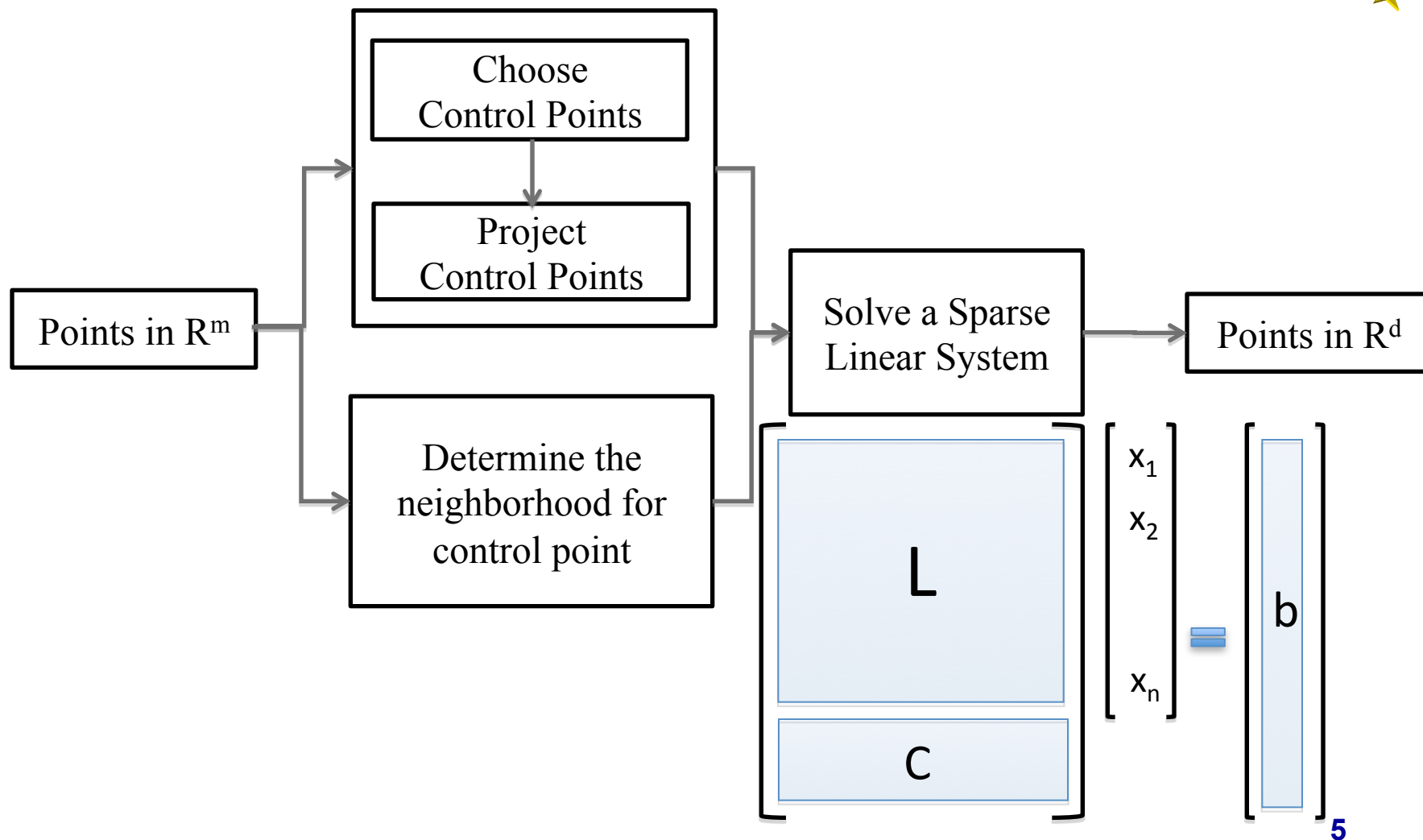
Multi Scalar Field

Questions

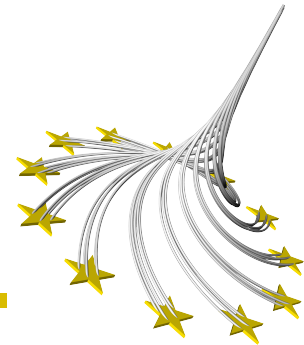
- Are there well-defined groups of similar objects?
- How are different groups related?
- What about instances within a group?
- Which data features determine the grouping?



Least Square Projection (LSP)

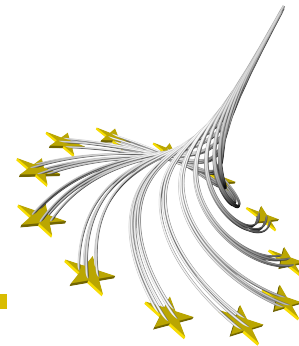


Extending LSP to 3D



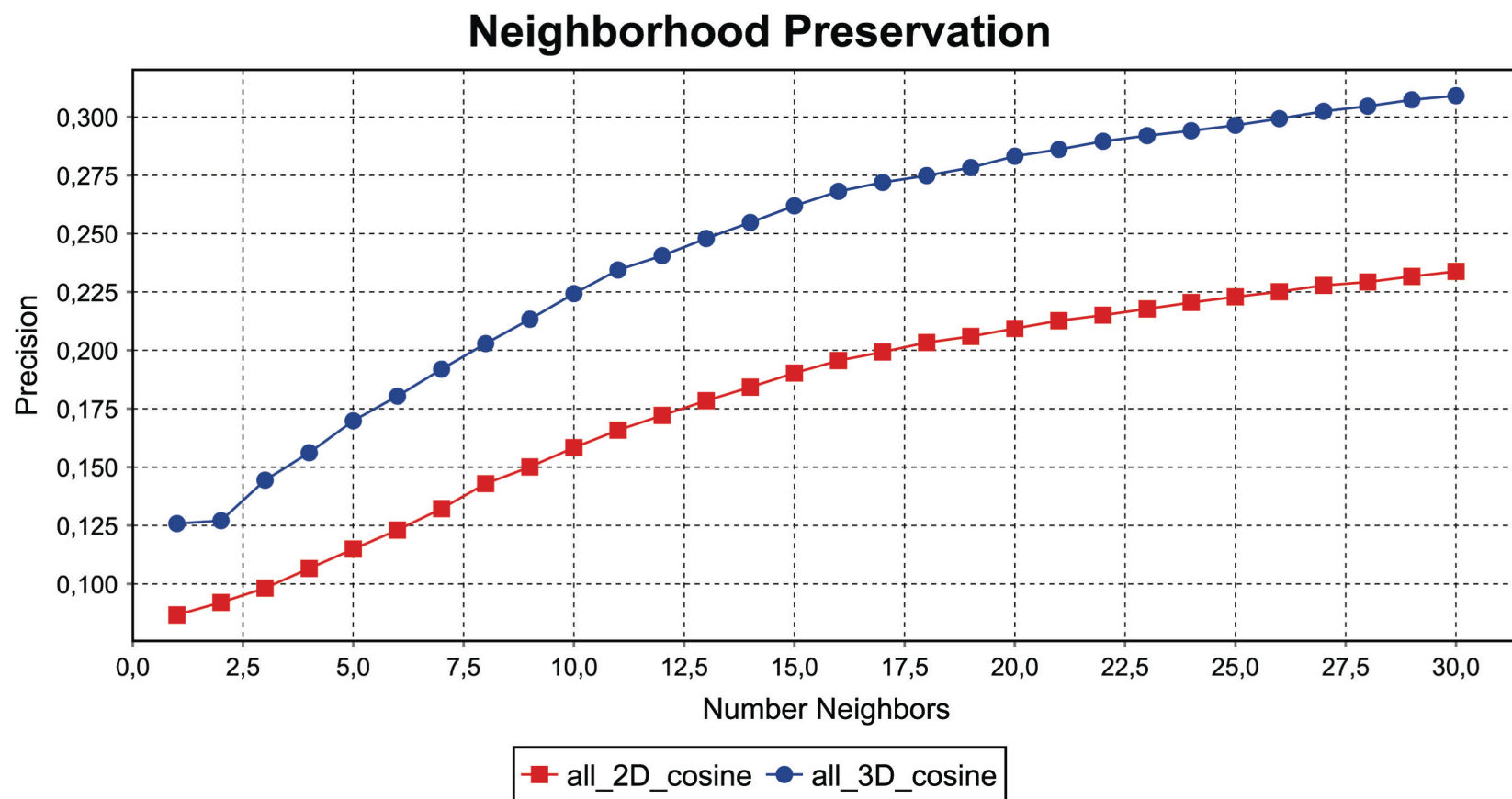
$$\begin{bmatrix} L \\ C \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix} = \begin{bmatrix} b \end{bmatrix}$$

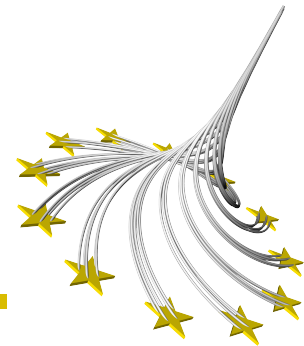
- This system is solved for each dimension in visual space.
- In 3D case, we need to solve 3 linear systems.



LSP 3D: Quantitative Evaluation

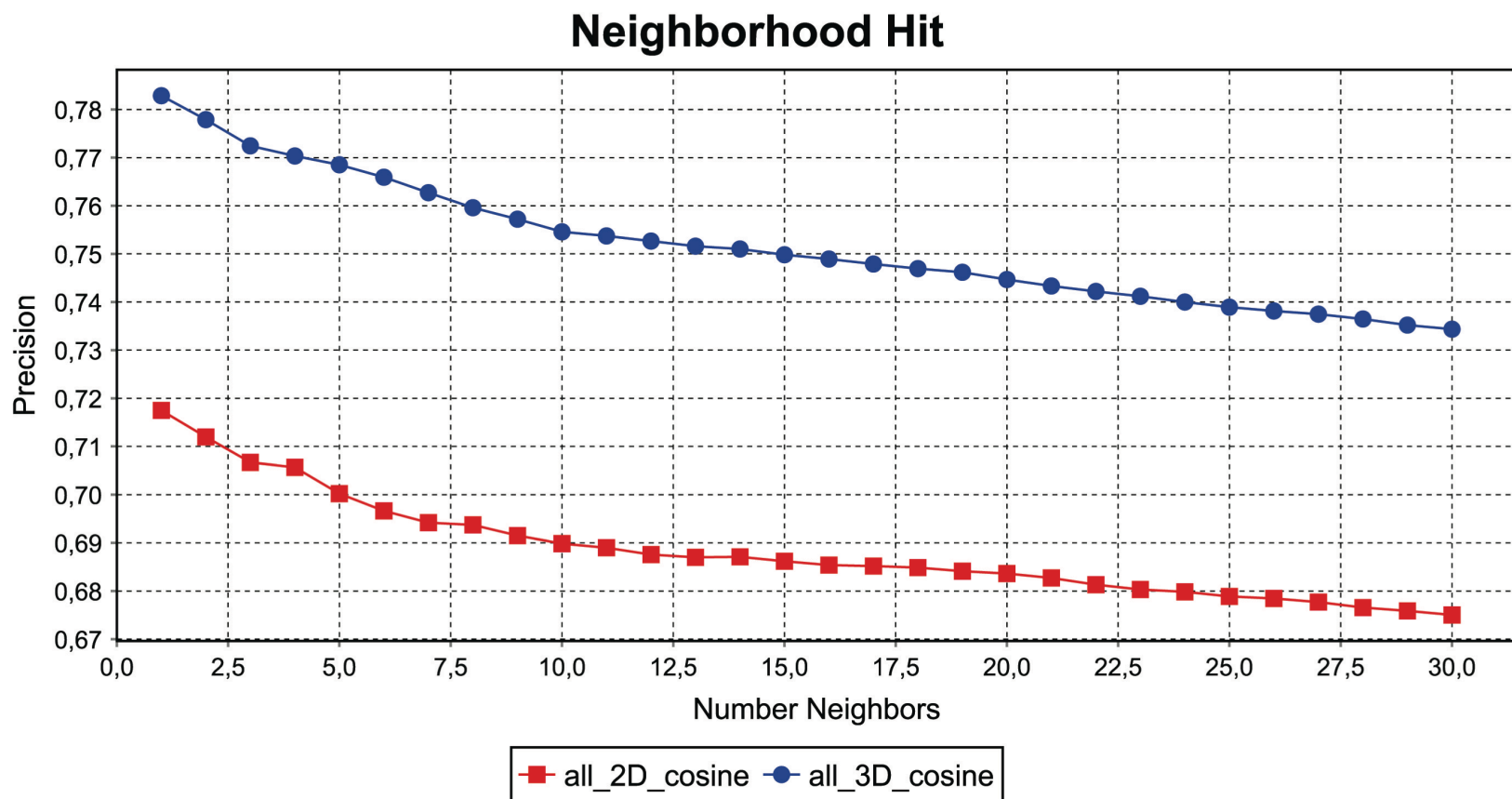
Neighborhood preservation - neighborhood after projection



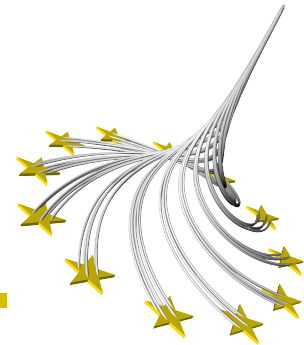


LSP 3D: Quantitative Evaluation

Neighborhood Hit – neighbors' classes after projection

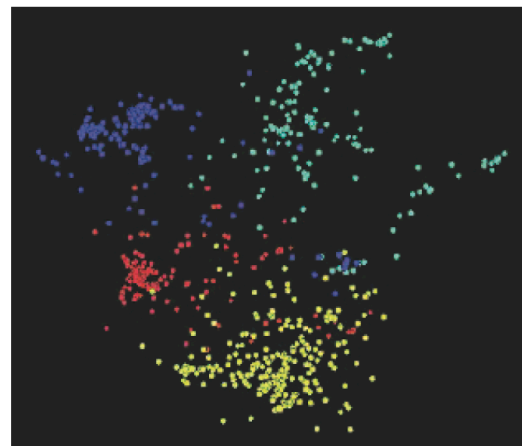


3D Cluster Visualization

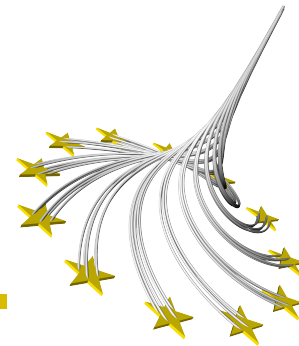


Color coded:

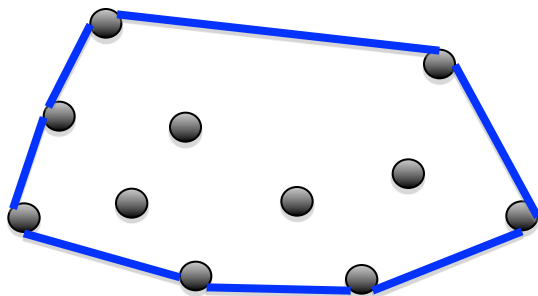
- ✓ Fast and robust.
- ✗ Loss in perception of depth .



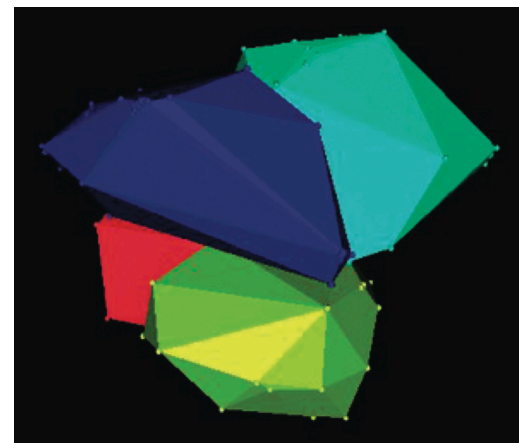
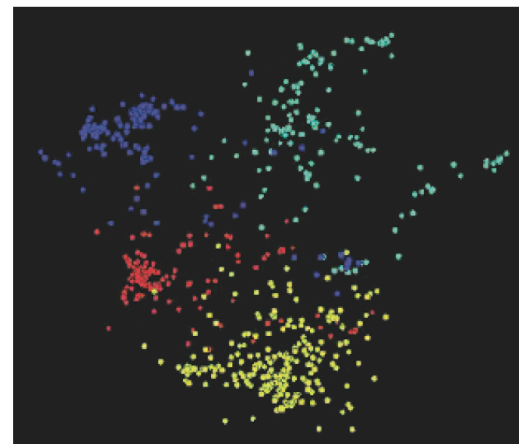
3D Cluster Visualization



Convex Hull:

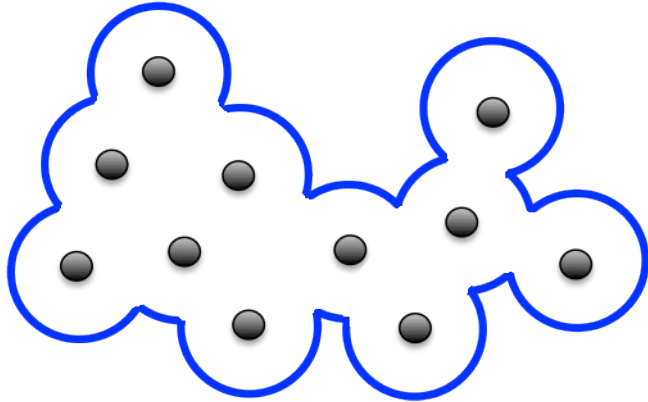


- ✓ Fast, robust and simple meshes.
- ✓ Effective in convex clusters.
- ✗ Misinterpretation in non-convex clusters.

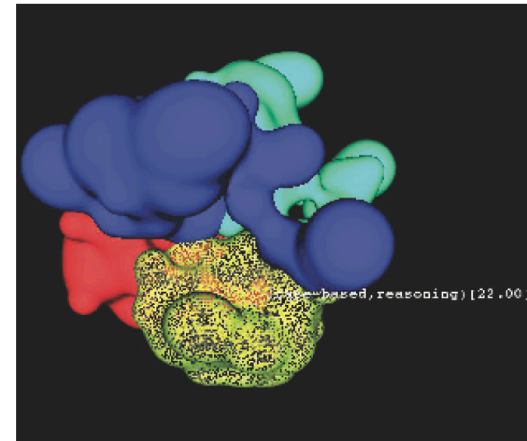
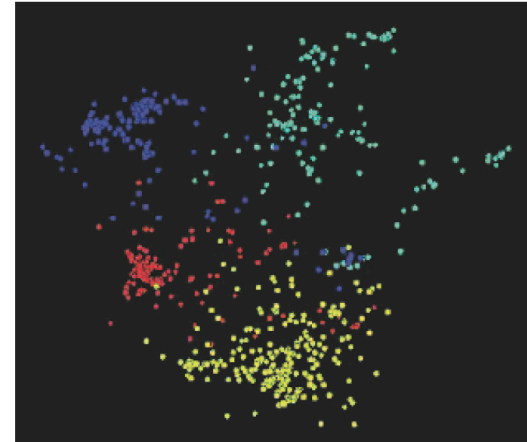
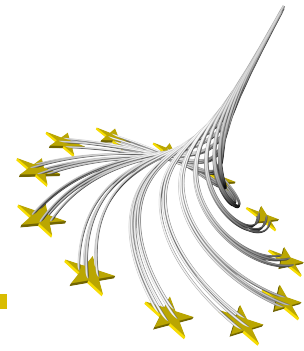


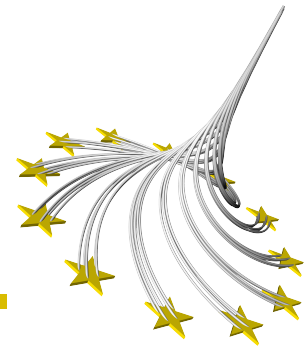
3D Cluster Visualization

Enclosing Surface iso-distance
to cluster points:



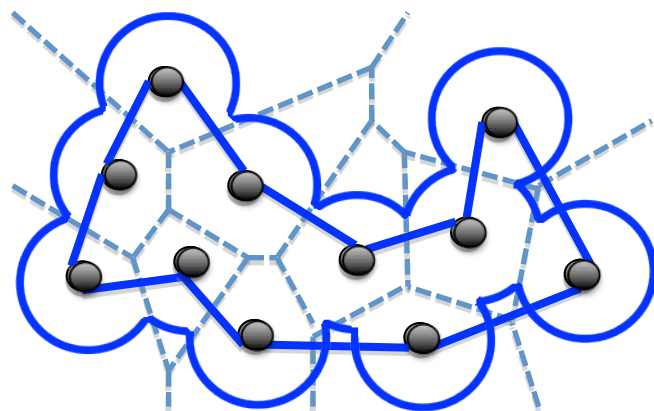
- ✓ Works for non-convex clusters.
- ✓ Visually pleasing rendering.
- ✗ Adaptive adjustment of the radius of influence when clusters come close to each other.



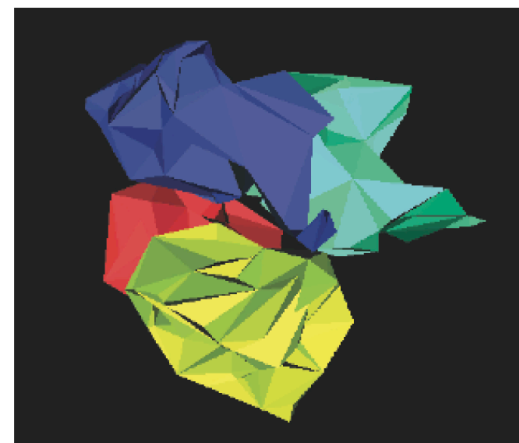
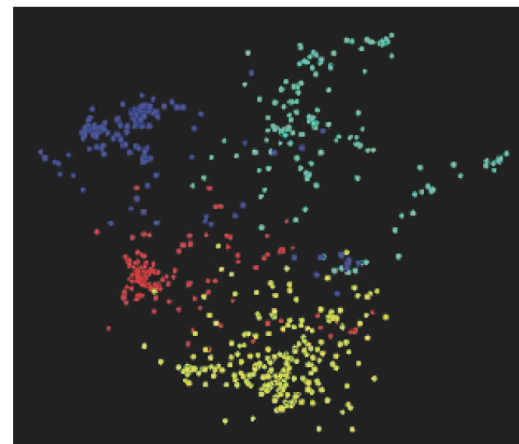


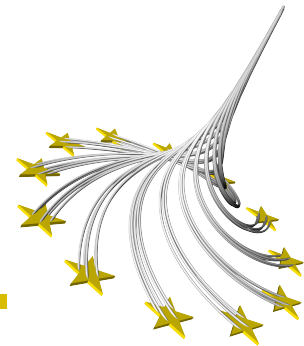
3D Cluster Visualization

Non-Convex Hull:



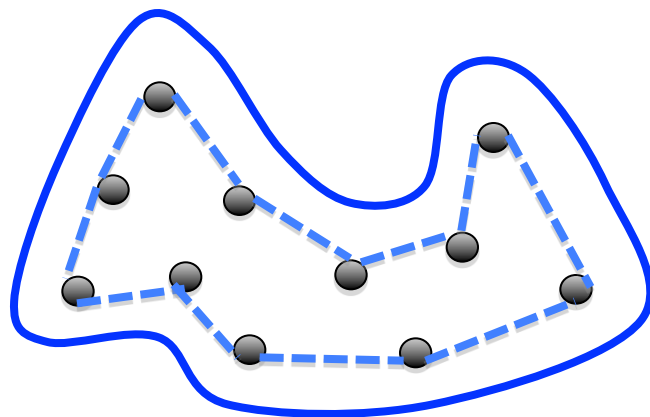
- ✓ Doesn't need radius adjustment.
- ✓ A distance field is created computing Voronoi diagram in GPU
- ✓ Works for non-convex cluster.



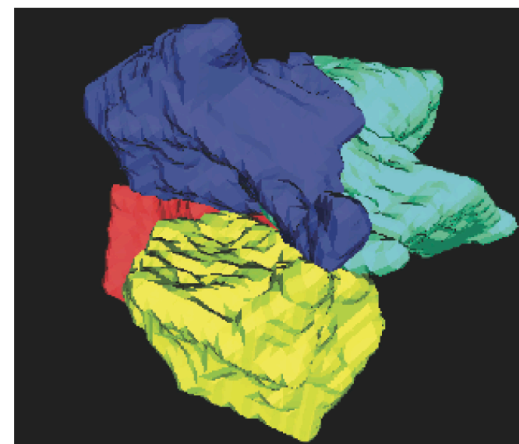
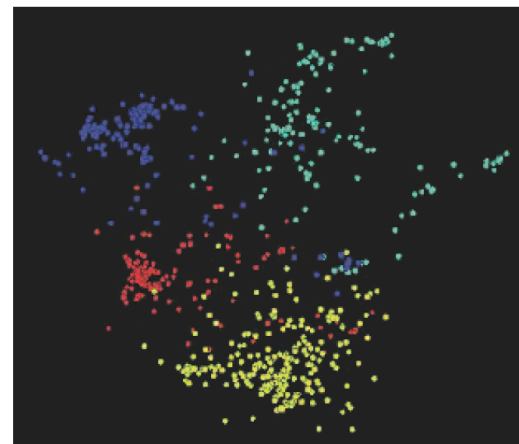


3D Cluster Visualization

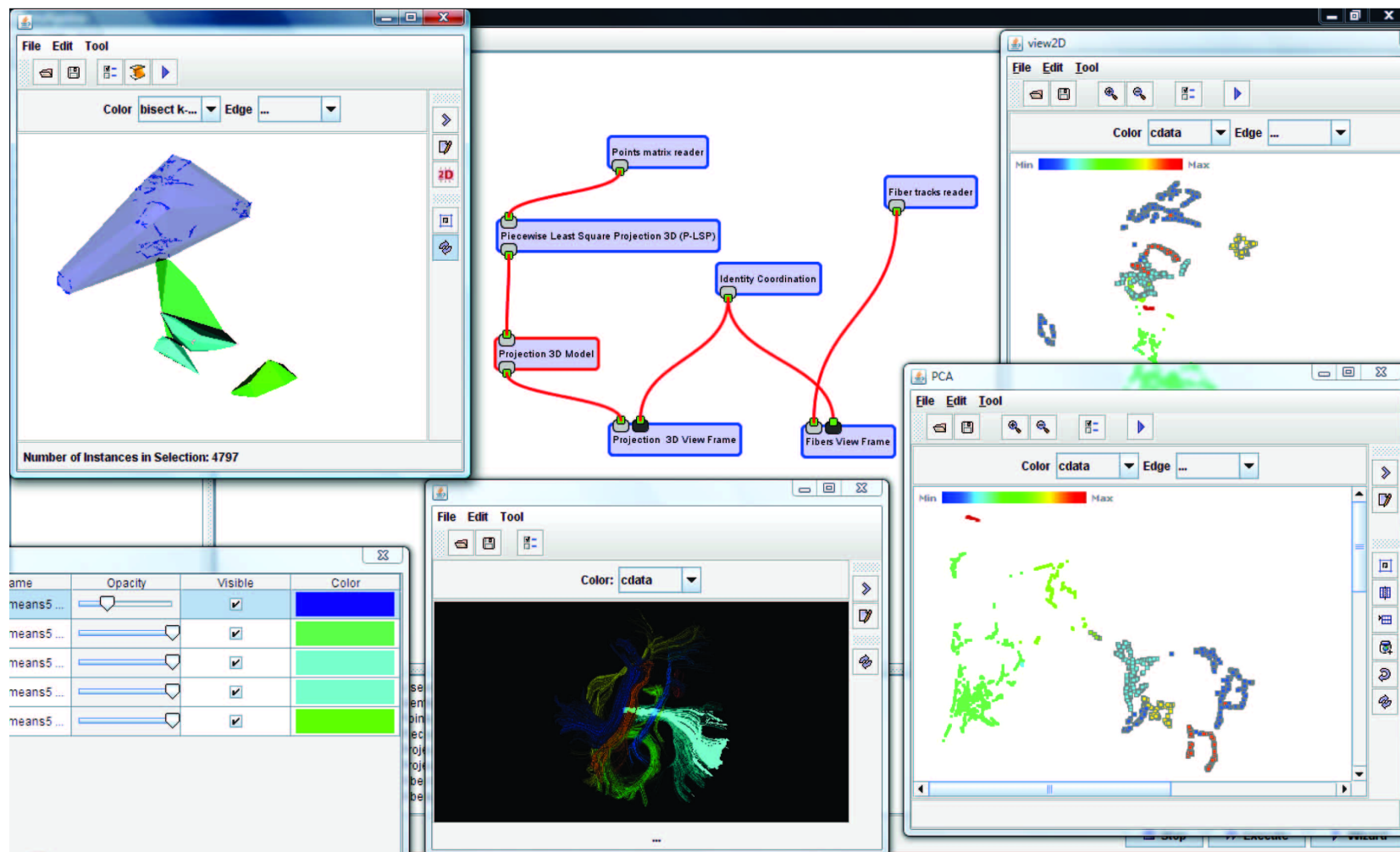
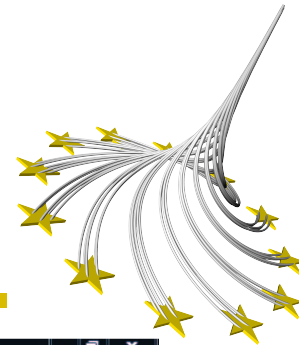
**Enclosing surfaces iso-distance
to non-convex Hull:**

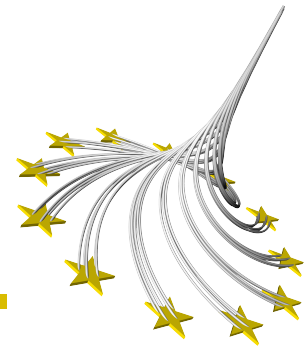


- ✓ Doesn't need radius adjustment.
- ✓ A distance field is created computing Voronoi diagrams in GPU
- ✓ Works for non-convex cluster.



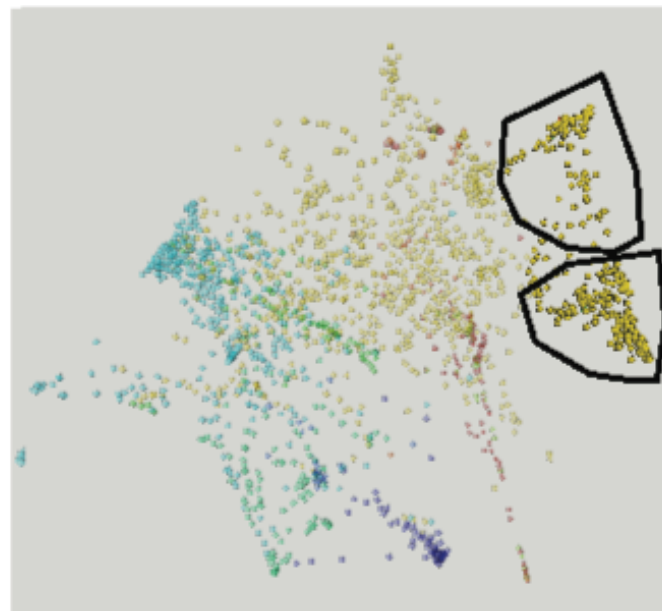
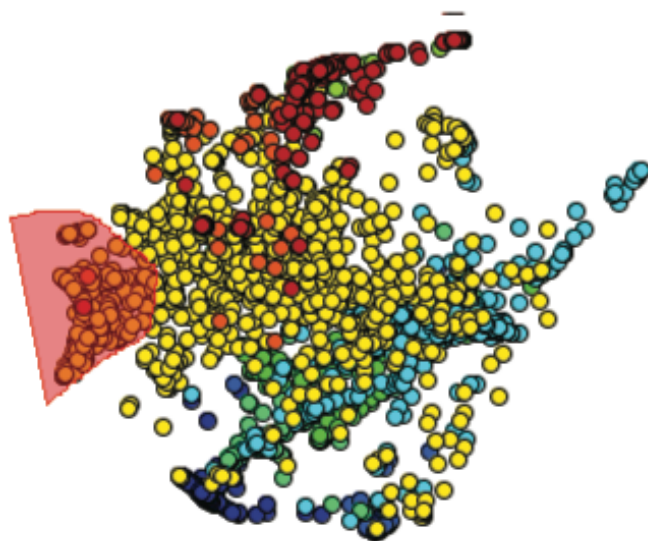
The System



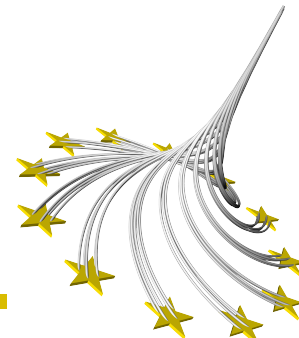


Coordination of 2D and 3D views.

- From 3D to 2D: selecting enclosing surface.
- From 2D to 3D: selecting well “resolved” groups that are preserved in both spaces.
- From 2D to 3D: selecting hidden groups

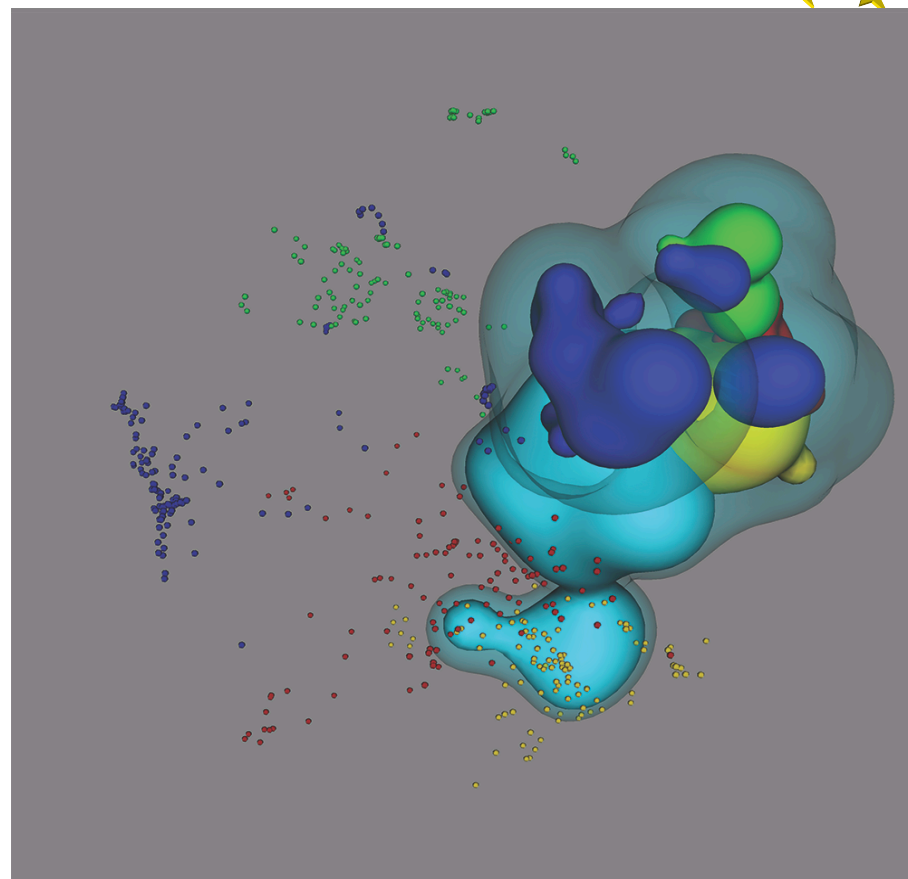


Hierarchy Clustering

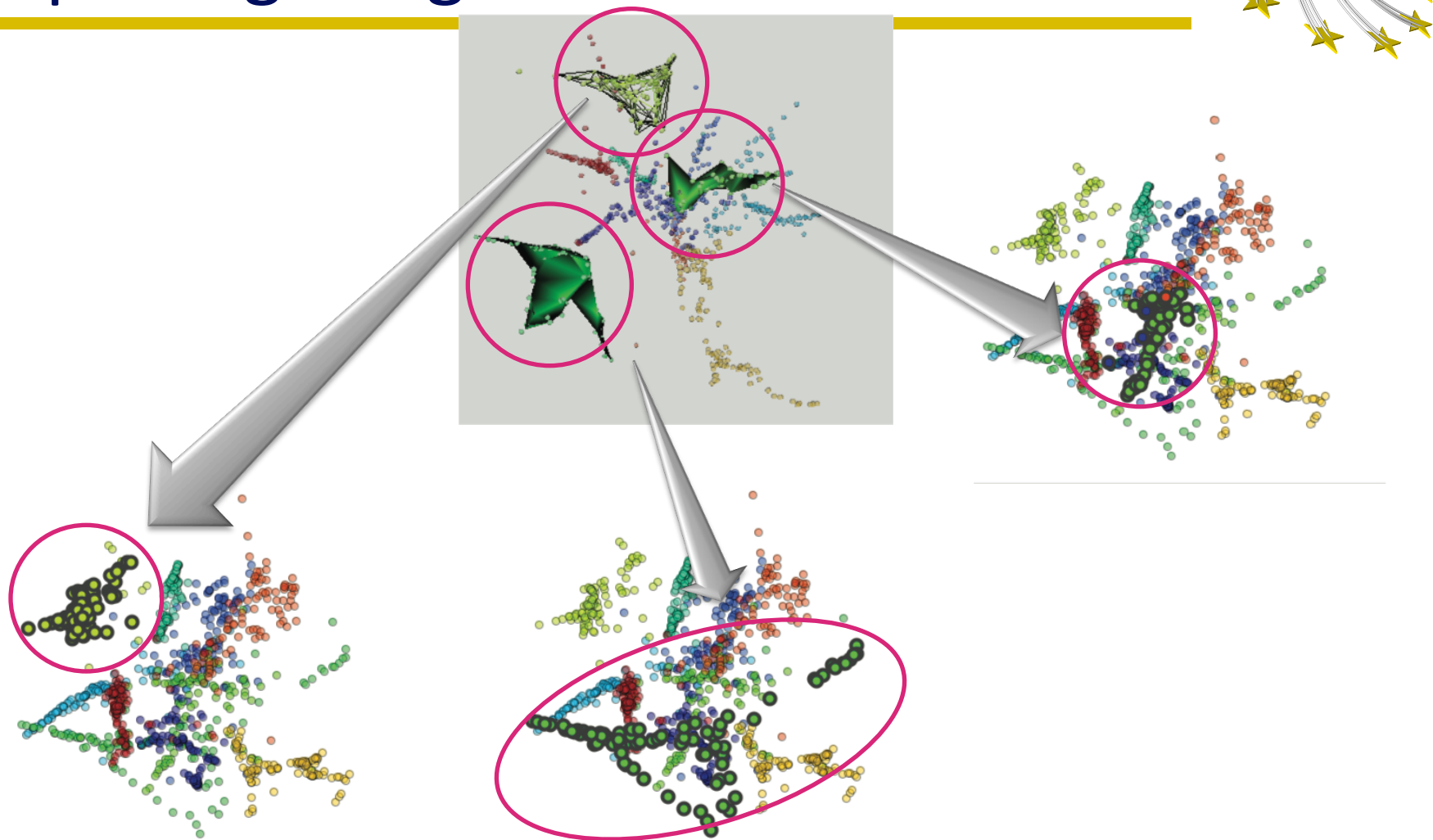


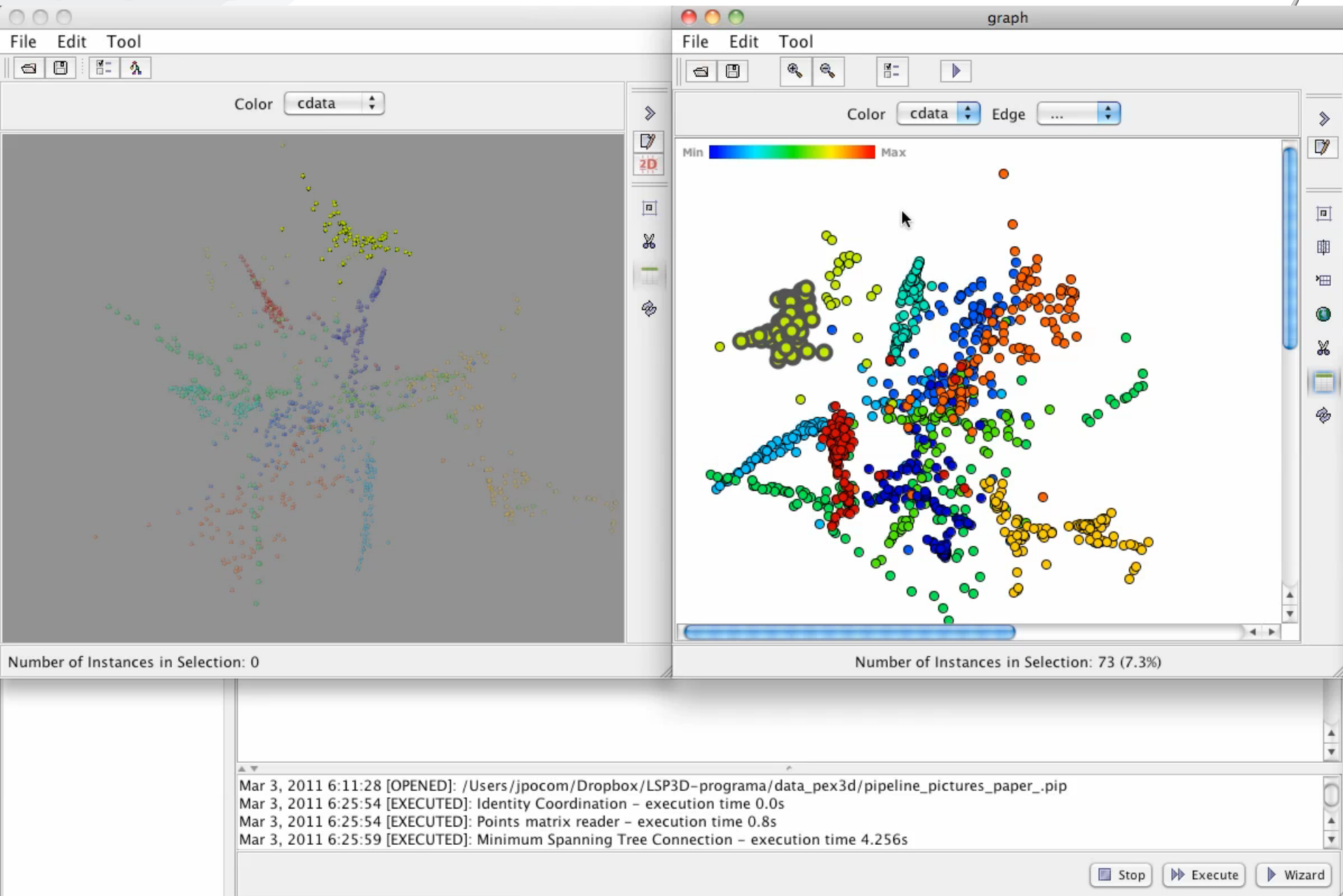
■ Root

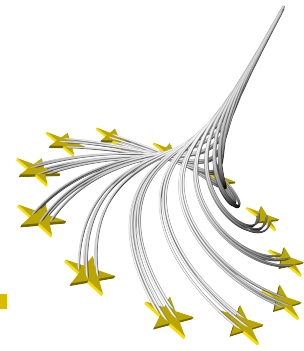
- (music, audio, proc, signal, int)[50.55]
- ▼ ■ (logic, program, induct)[30.51]
 - (inform, retriev)[55.58]
 - (case-bas, reason, learn)[17.91]
 - (learn, algorithm, comput, queri, statist)[48.70]
 - (logic, program, learn, induct, muggleton)[22.94]
 - (logic, program)[30.77]
- (inform, retriev)[68.22]
- (reason, case-bas)[23.74]
- (case-bas, reason)[25.70] (network, rout, wireless,



Exploring image sets



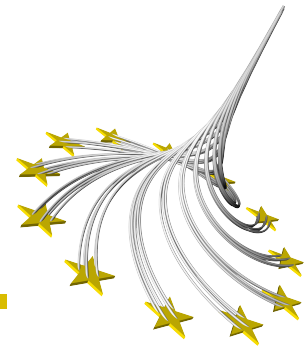




Evaluation user study set up

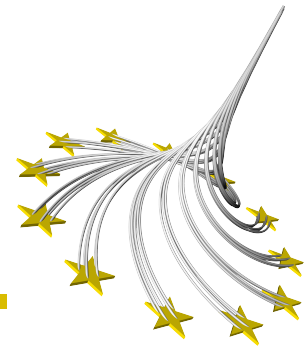
- 12 participants
- Experience with computers
- Short training session
- 2 datasets
 - Document data (681 objects, 2993 dimensions)
 - Medical imaging data (1000 objects, 150 dimensions)

Quality Measures

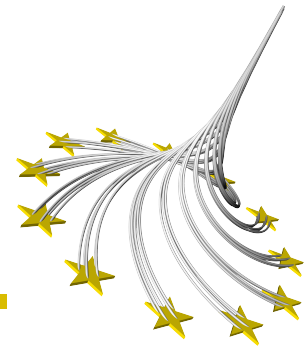


- | | | |
|---------------------|---|---------------------|
| • Reliability | ➡ | • Correctness |
| • Efficiency | ➡ | • Response time |
| • Learn ability | ➡ | • User satisfaction |
| • User-friendliness | ➡ | • User preferences |

Set Up

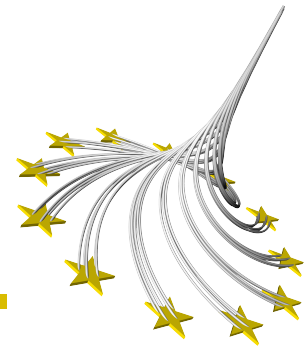


- Set of tasks
- Record time
- Participants confidence using Likert scale
- User preference



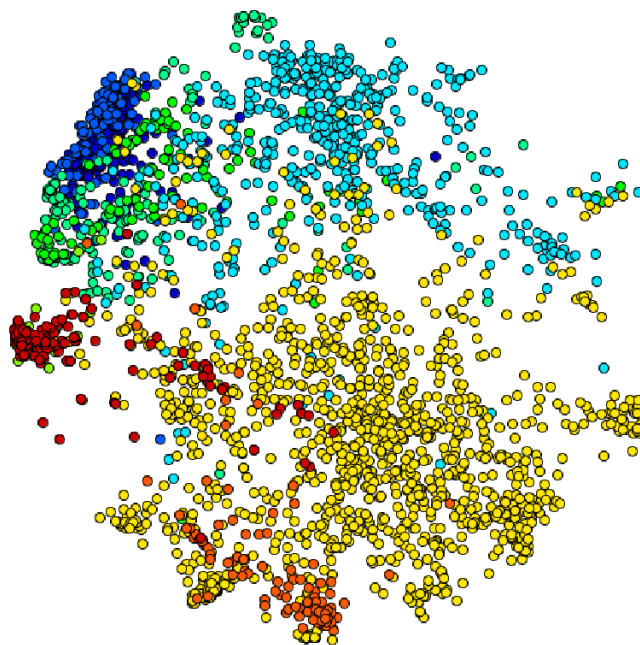
Statistical Significance

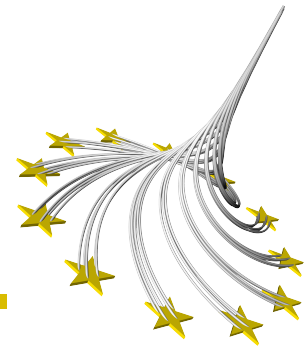
- Shapiro-Wilk test against normal distribution
- 2 projections
 - Wilcoxon Matched-Pairs Signed-ranks test
 - T-test
- 5 cluster visualizations
 - Friedman's χ^2 -test or test for repeated measures
 - ANOVA test



2D vs. 3D Hypotheses

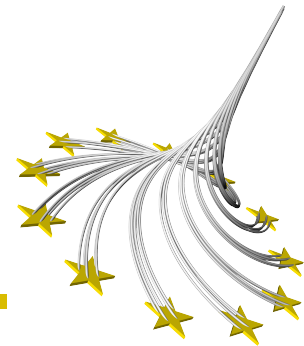
- Data were clustered before projection
- Two hypotheses were formulated
 - 2D projec to find in 3D.
 - 3D projec ration leading to more corr



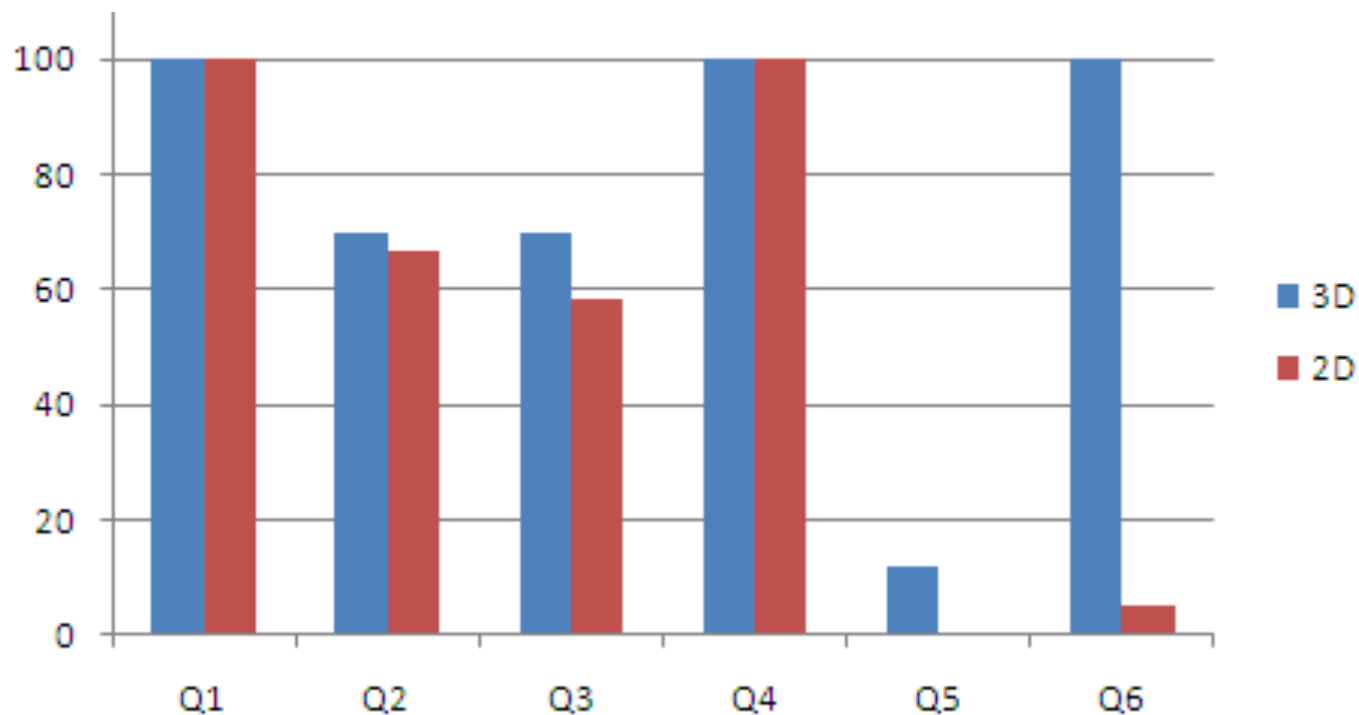


Tasks

- 1) Count the clusters
- 2) Order the clusters by their density
- 3) List all overlaps of clusters
- 4) Detect an object within a cluster
- 5) Find closest cluster to a specific point
- 6) Repeat Task 5 with a different point



Correctness 2D vs. 3D



The user's perception on detecting the similarities among clusters.

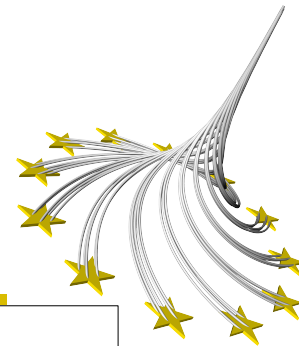
Q3

Q5

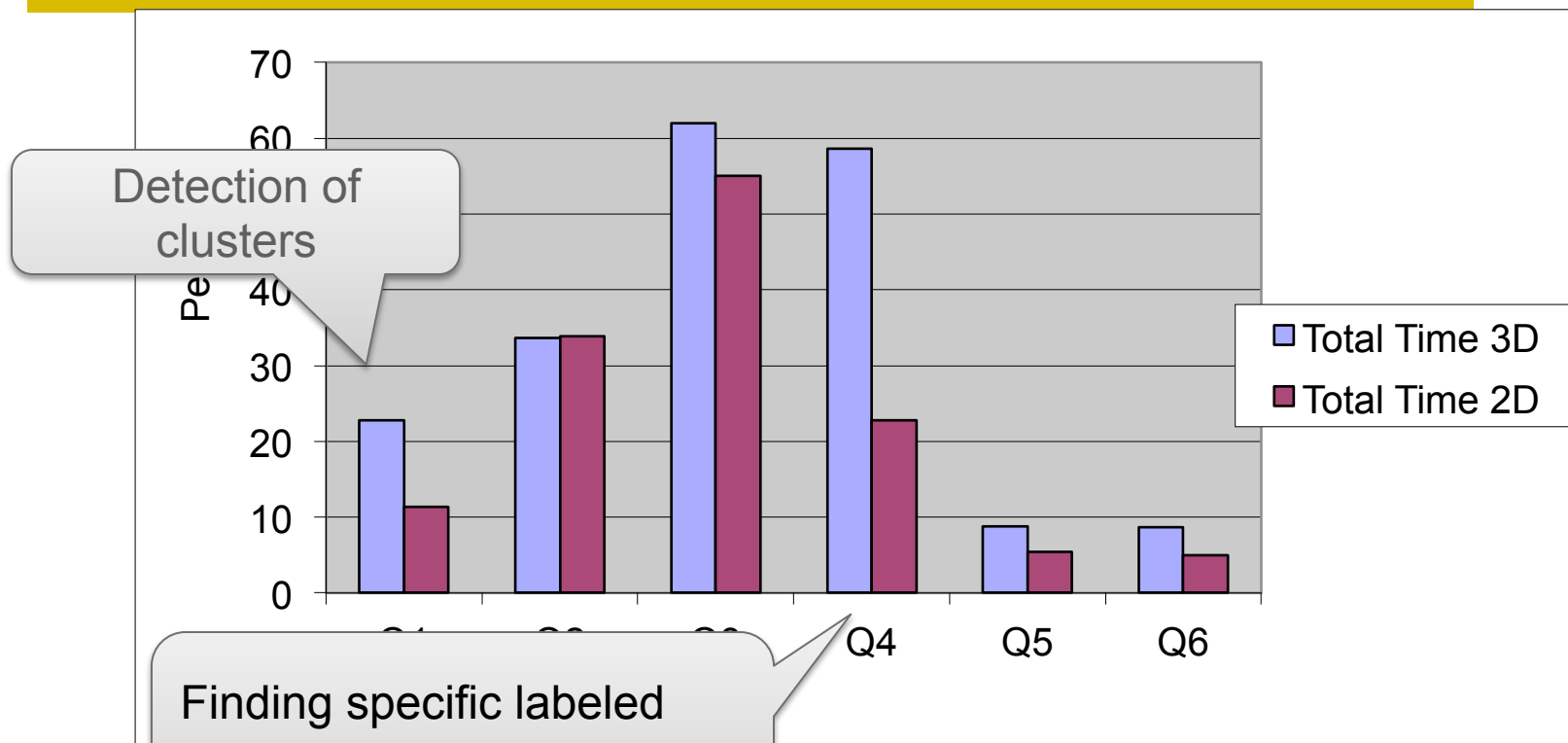
Q6

0.01562

0.01953



Response Times 2D vs. 3D

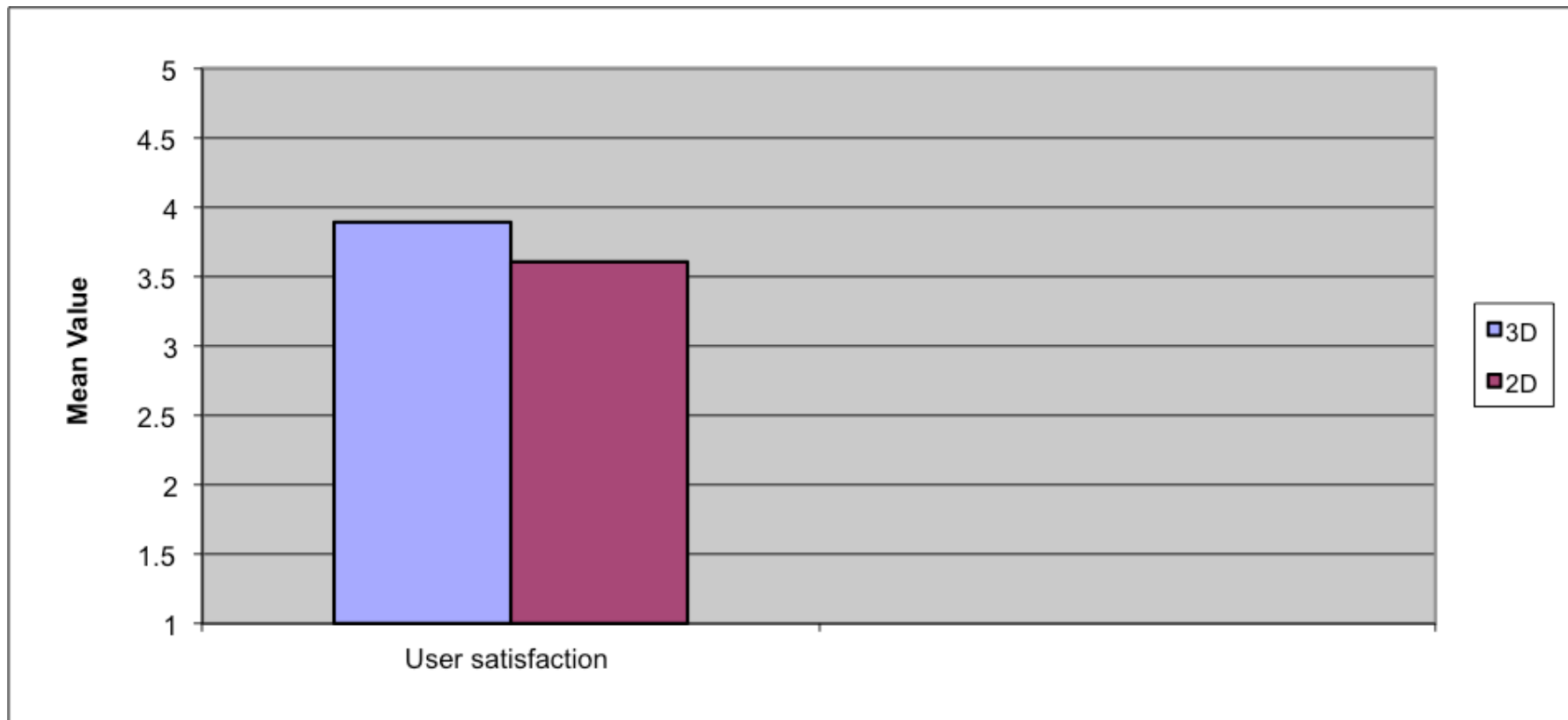
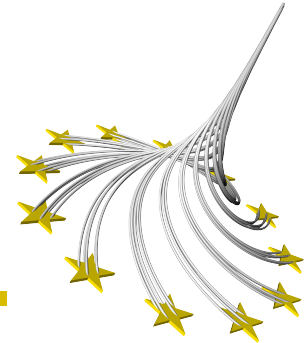


	Q1	Q2	Q3	Q5	Q6
Asymp. Sig.	0.01855	0.8501	0.5186	0.375	0.4922

Mean 58.58 22.75

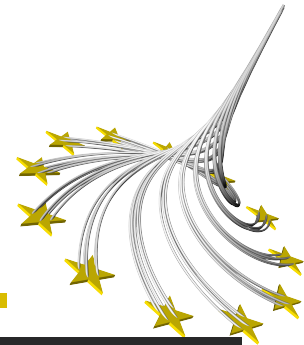
The two-tailed P value equals 0.0189

User Satisfaction

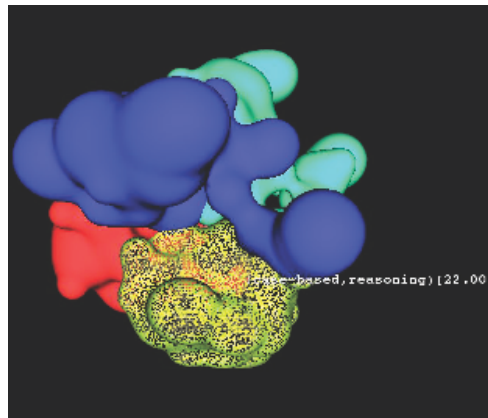


	3D vs. 2D
Asymp. Sig.	0,007812

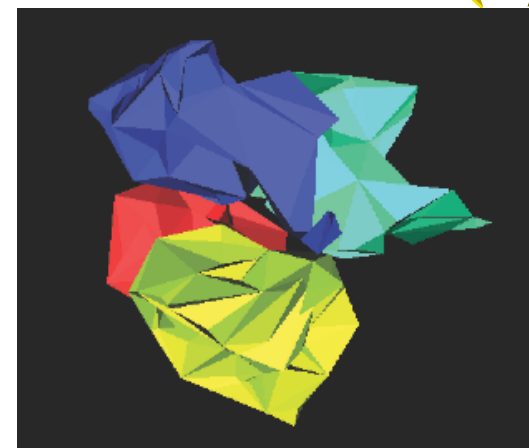
User Study Evaluation Cluster Visualization



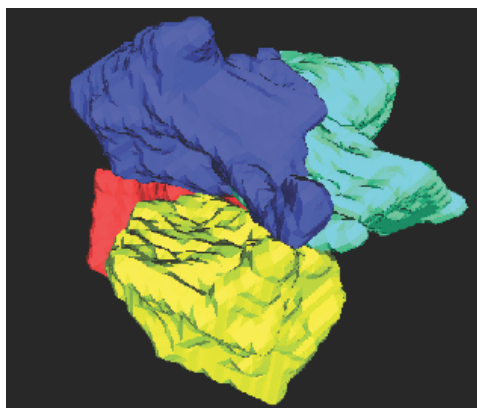
convex hull



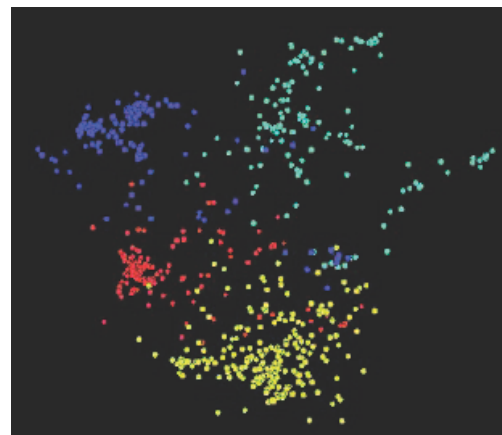
**enclosing surfaces
isodistant to points**



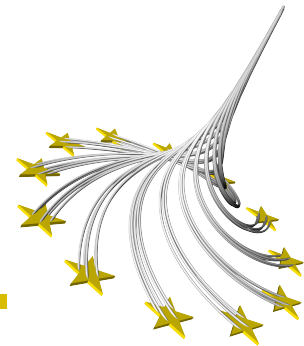
non-convex hull



**enclosing surfaces isodistant
to non-convex hull**



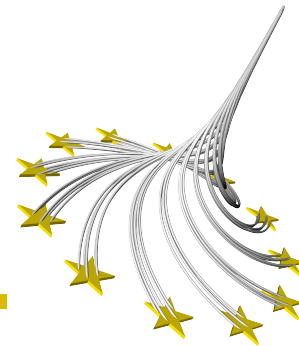
color-coded point cloud.



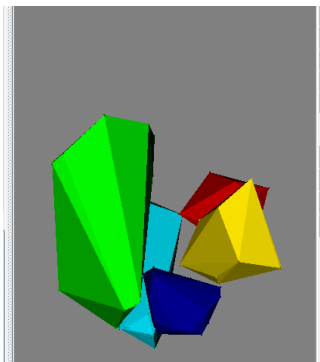
Tasks

- 1) Count the clusters
- 2) List cluster overlaps
- 3) Identify most distant clusters

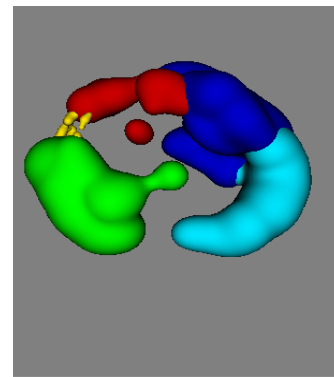
Set up



- Different techniques coupled with different datasets
- Half of the participants complementary combinations to the other half

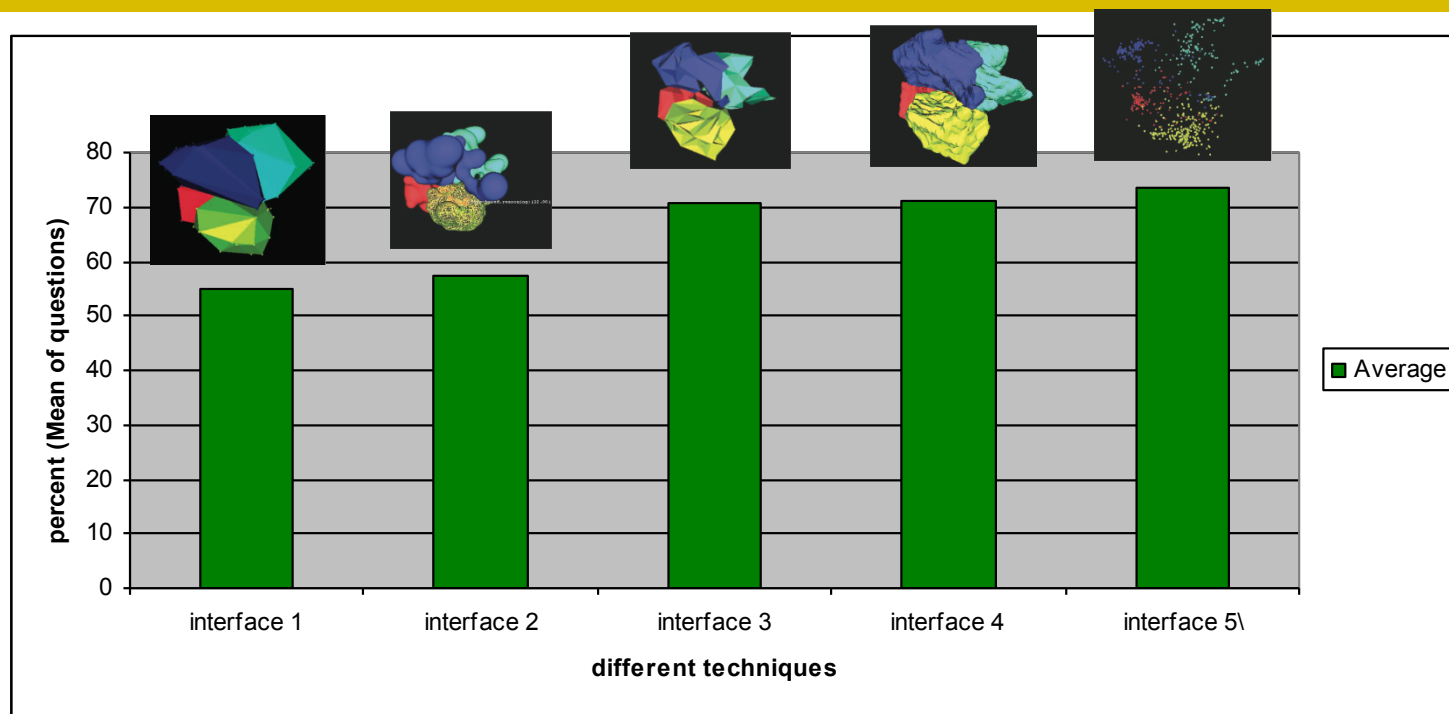
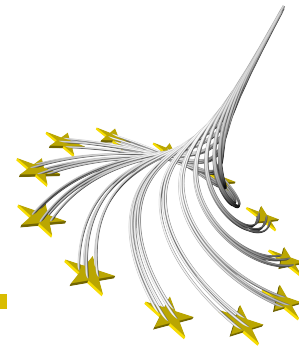


Document data, 5 classes



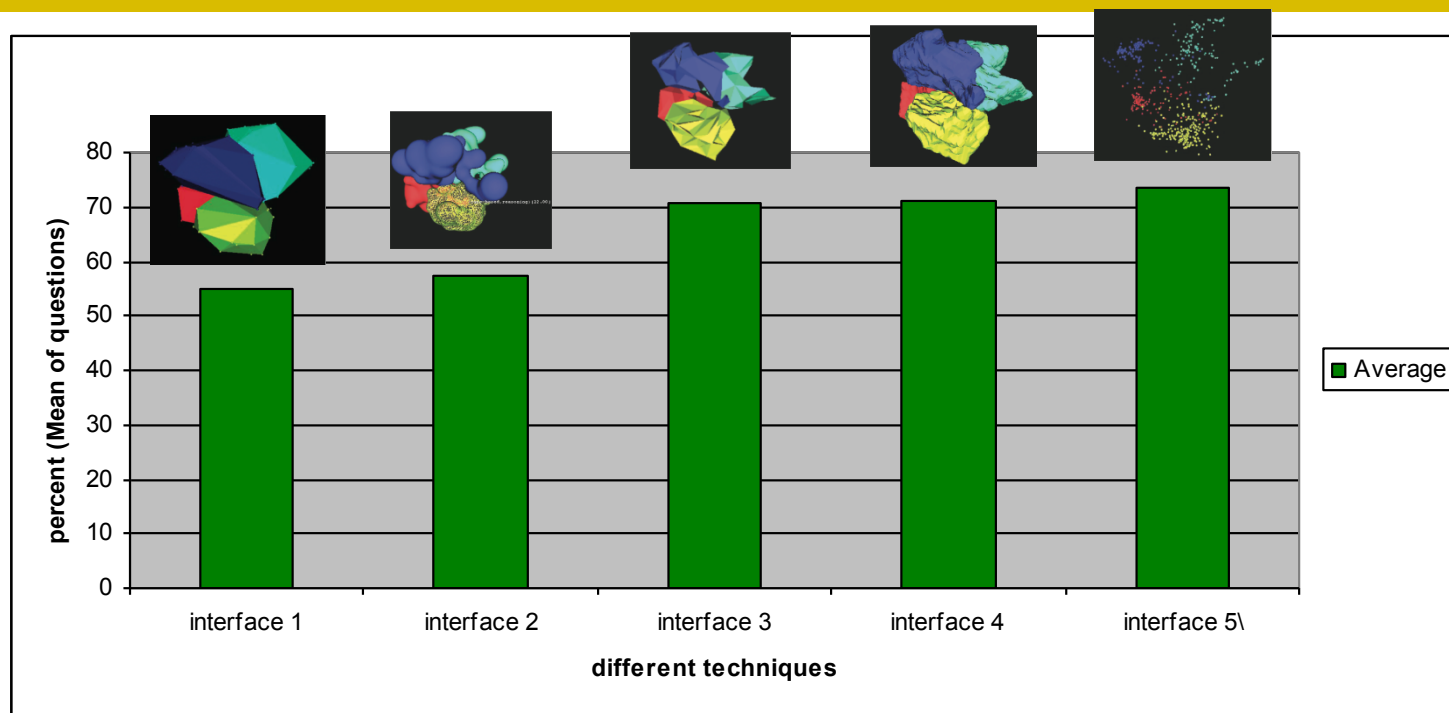
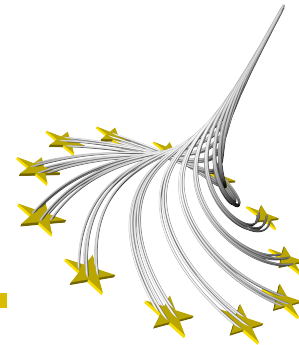
Medical data, 12 classes

Correctness



No significant difference

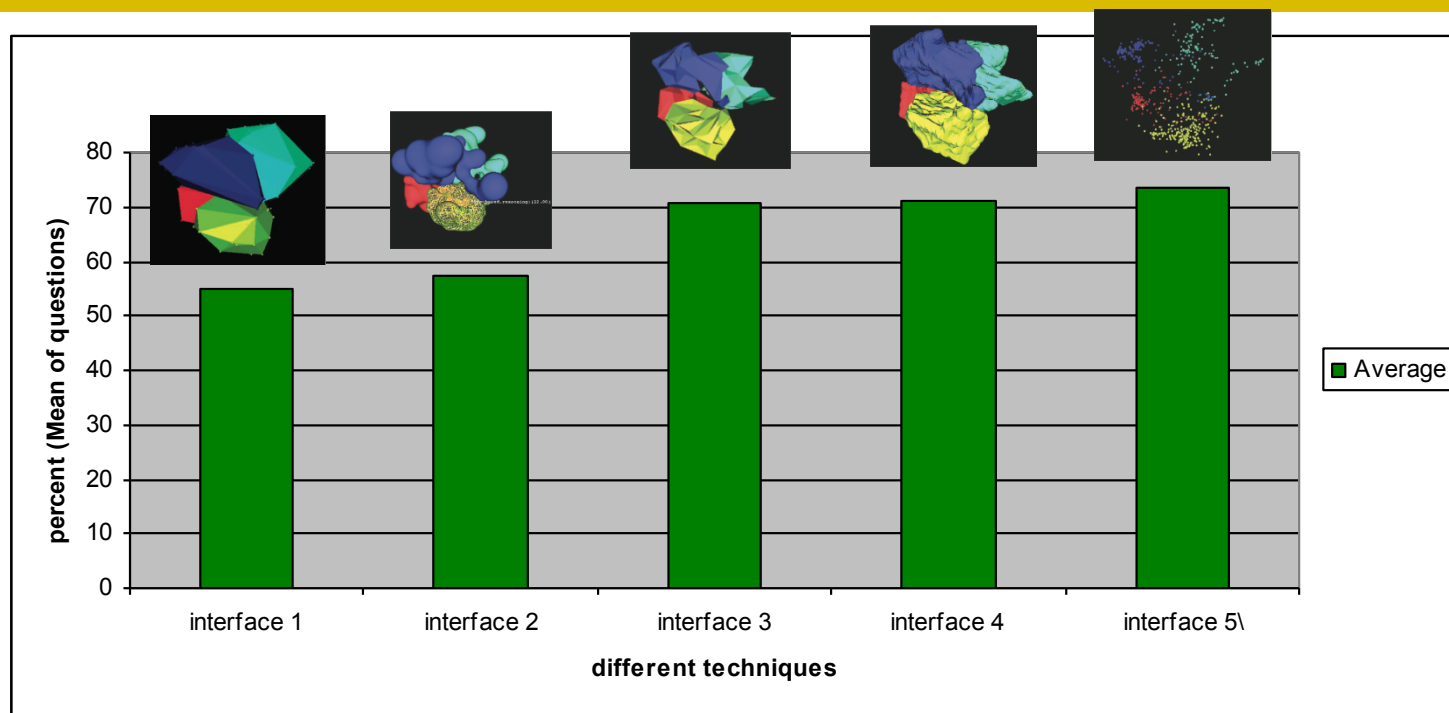
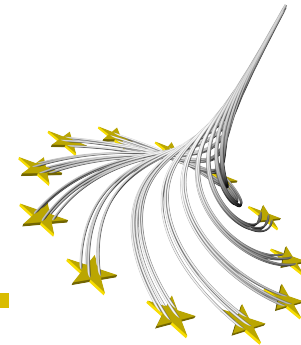
Correctness



	Q2	Q3
Friedman's Chi-Square	11.24	6.8
Asymp. Sig.	0,025	0,149

Document Dataset

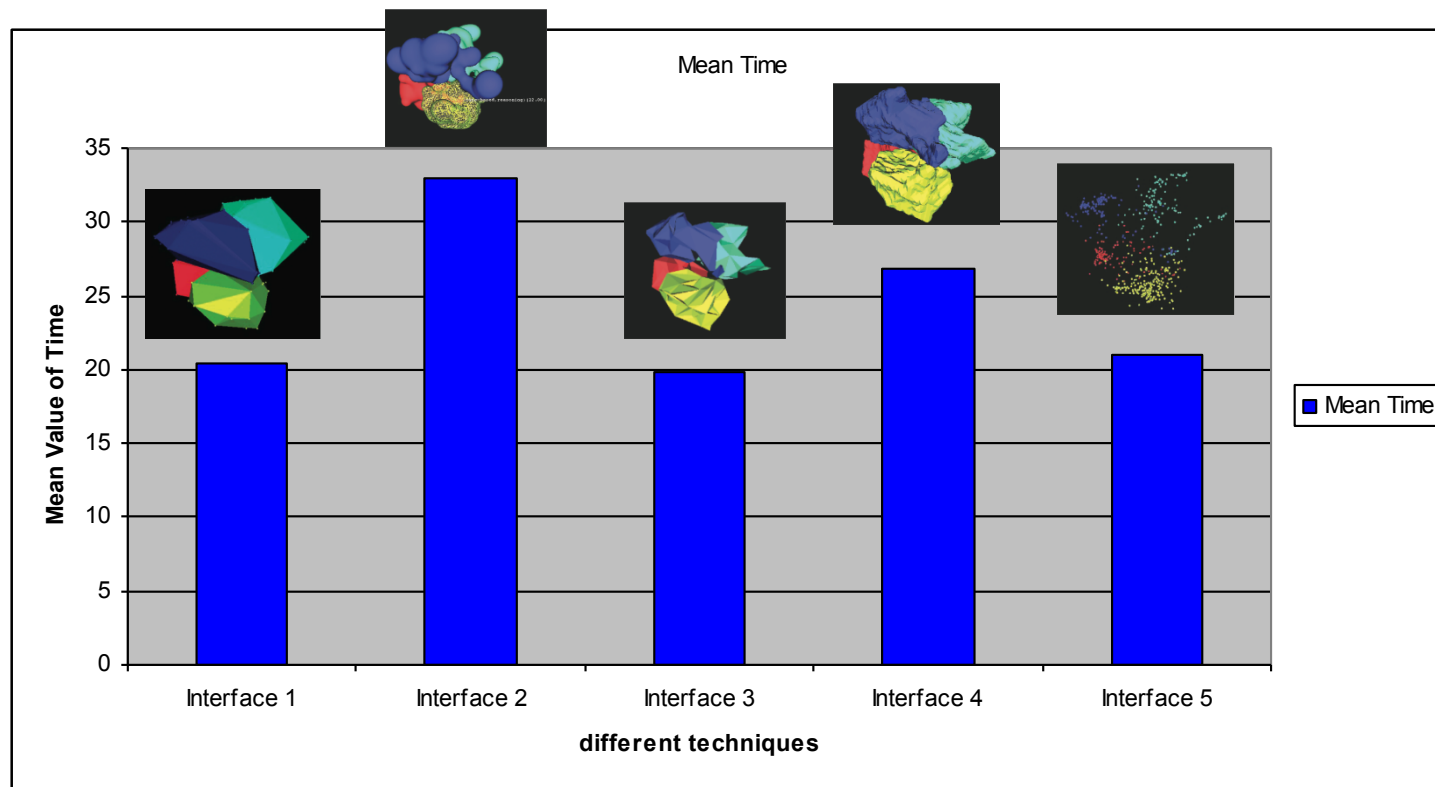
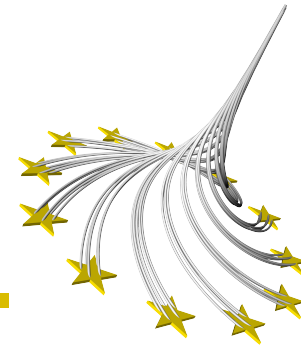
Correctness



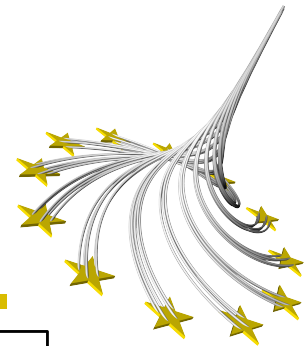
	Q2	Q3
Friedman's Chi-Square	9	2, 5
Asymp. Sig.	0,063	0,645

Medical Image Dataset

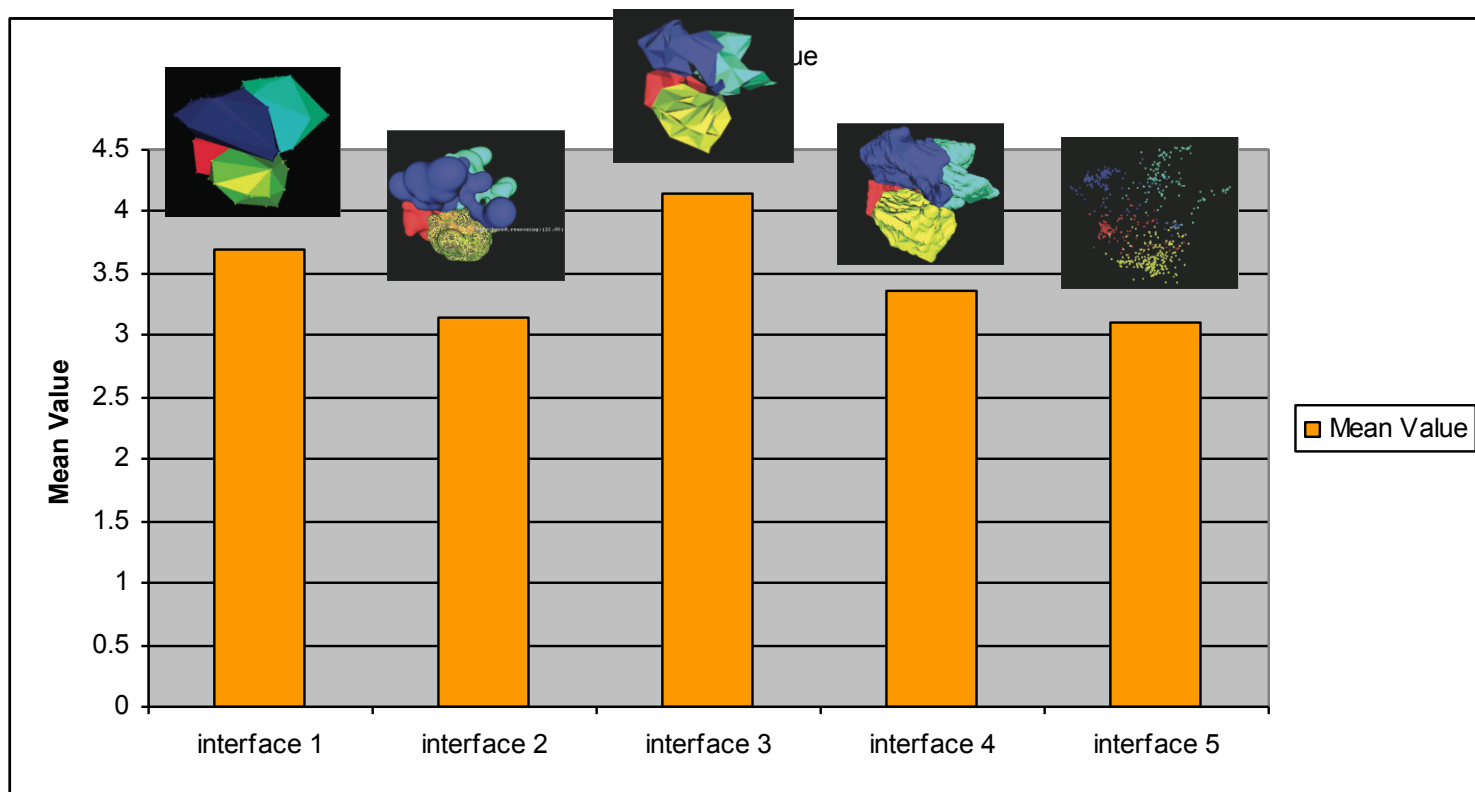
Response Time



Anova Probability = 0.022
Less Accurate
Longer Time

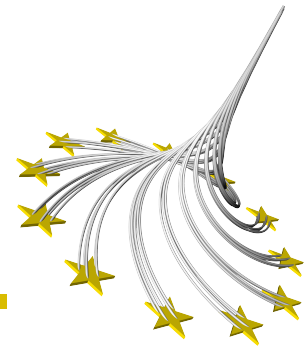


User Satisfaction



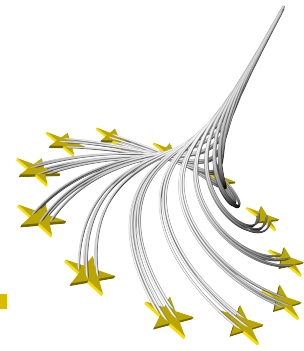
Lowest User Satisfaction
Highest rate of satisfaction

No significant difference



Conclusion

- Framework for multidimensional data visualization
- 3D projection
- 3D cluster visualization
- Quantitative evaluation for 2D vs. 3D projection
- Higher precision in 3D
- User study for 2D vs. 3D
- Higher correctness & user satisfaction in 3D
- User study different cluster visualization



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<http://infoserver.lcad.icmc.usp.br/infovis2/Tools>